

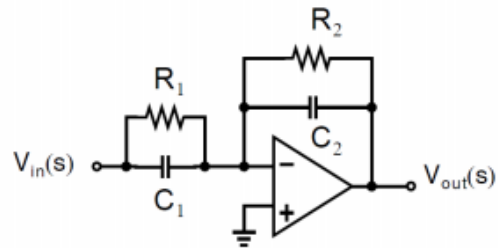
1.

$$V_{out}(s) = \frac{-1}{sC_2} \left[\left(\frac{1}{R_1} + sC_1 \right) V_{in}(s) + V_{out}(s) / R_2 \right]$$

$$\frac{V_{out}(s)}{V_{in}(s)} = -\frac{R_2}{R_1} \frac{1 + R_1 C_1 s}{1 + R_2 C_2 s}$$

The opamp has a frequency response

$$A(s) = \frac{A_0}{1 + \frac{sA_0}{\omega_{ia}}}$$



Denoting the negative opamp input terminal voltage, V_x , we may write a nodal equation there as follows:

$$\frac{V_{in} - V_x}{R_1 \parallel 1/sC_1} = \frac{V_x - V_{out}}{R_2 \parallel 1/sC_2}$$

Substituting in $V_{out} = -A(s)V_x \Rightarrow V_x = -V_{out} / A(s)$:

$$\frac{V_{in} + V_{out} / A(s)}{R_1 \parallel 1/sC_1} = \frac{-V_{out} / A(s) - V_{out}}{R_2 \parallel 1/sC_2}$$

Using the expression for $A(s)$ above and rearranging yields:

$$\frac{V_{out}(s)}{V_{in}(s)} = -\frac{R_2}{R_1} \frac{A_0}{1 + A_0} \frac{1 + R_1 C_1 s}{1 + R_2 C_2 s} \frac{1}{1 + s / \omega_{ia}}$$

2. KCL at C_1 : $-gm_1.V_1 - gm_2.V_2 + gm_4.V_o = sC_1.V_2$

KCL at C_2 : $-gm_3.V_2 = sC_2.V_o$

$H_o(s) = V_o/V_1 = gm_1.gm_3 / (s^2.C_1.C_2 + s.gm_2.C_2 + gm_3.gm_4)$

$H_1(s) = V_2/V_1 = (-sC_2 / gm_3) H_o(s) = -sC_2.gm_1 / (s^2.C_1.C_2 + s.gm_2.C_2 + gm_3.gm_4)$

3. By interreciprocity, $V_o = - \sum I'_k V_k$. Using Bashkow's method, we assume $I'_1 = 1$ A, and also to simplify the calculations, $R = 1$ (this doesn't change the voltage gain). Then $V_a' = 2$, $I_2' = 2$, $I_b' = 3$, $V_b' = 5$, $I_3' = 5$, $I_c' = 8$, $V_c' = 13$, $I_4' = 13$, $I_d' = 21$.

Hence, the scale factor is $-1/21$, and $V_o = (1/21) [1 \times 1 + 2 \times 1 + 5 \times 2 + 13 \times 2] = 39/21 \sim 1.857$ V.

